CZECH TECHNICAL UNIVERSITY IN PRAGUE
Faculty of Electrical Engineering
Department of Measurement

Application of Magnetic Sensors for Navigation Systems

DOCTORAL THESIS

2007 **Jan Včelák**

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