

# **The Retirement Decision in Germany**

## **-A Dynamic Programming Approach-**

Inaugural-Dissertation  
zur Erlangung des akademischen Grades  
eines Doktors der Wirtschaftswissenschaft  
des Fachbereichs Wirtschaftswissenschaft  
der Freien Universität Berlin

vorgelegt von

Diplom-Volkswirt  
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Zweitgutachter: Professor John Rust, PhD

Tag der Disputation: 18. Juli 2002  
Diese Version: Berlin, Februar 2003

Berichte aus der Volkswirtschaft

**Thomas Knaus**

**The Retirement Decision in Germany**

-A Dynamic Programming Approach-

D 188 (Diss. Freie Universität Berlin)

Shaker Verlag  
Aachen 2003

Die Deutsche Bibliothek - CIP-Einheitsaufnahme

*Knaus, Thomas:*

The Retirement Decision in Germany. A Dynamic Programming Approach/  
Thomas Knaus.

Aachen : Shaker, 2003

(Berichte aus der Volkswirtschaft)

Zugl.: Berlin, Freie Univ., Diss., 2002

ISBN 3-8322-1292-2

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Printed in Germany.

ISBN 3-8322-1292-2

ISSN 0945-1048

Shaker Verlag GmbH • P.O. BOX 101818 • D-52018 Aachen

Phone: 0049/2407/9596-0 • Telefax: 0049/2407/9596-9

Internet: [www.shaker.de](http://www.shaker.de) • eMail: [info@shaker.de](mailto:info@shaker.de)



# Acknowledgements

I have written this dissertational thesis while being a research and teaching assistant at the Institute of Public Finance and Social Policy at Freie Universität Berlin. I am thankful to my advisor Irwin L. Collier for his help and many valuable comments.

The main part of the project started out from a research stay at Yale University. I thank the German Academic Council (DAAD) for financial support. I am grateful to my second advisor John Rust for his encouragement and support, and to Hugo Benitez-Silva for his help and precious comments during the time at Yale and afterwards. I also thank them and Moshe Buchinsky for providing me parts of the program code used in this thesis.

I also thank the members of my dissertation committee, Irwin L. Collier, Helmut Bester, Lutz Kruschwitz, Jürgen Wolters, Anette Boom and Sven Schreiber.

I also benefitted from discussions with many colleagues and friends, in particular, Miriam Beblo, Andreas Göhler, Sebastian Kessing, Peter Kuhbier, Hans Meier, Hannah Nielsen, Robert Nuscheler, Christoph Reichle, Volker Schmitz, Rainer Schulz, Sabine Stephan, Thorsten Thadewald, Harald Uhlig, Amelie Wolf and Jürgen Wolters.

I am thankful for helpful comments from seminar and conference participants at Helenenau, Aarhus and Bilbao.

I am especially grateful to Inez Weidinger for inspiring discussions and patient support.

Berlin, February 2003



To my parents



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