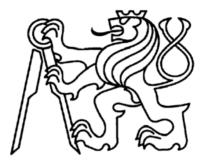
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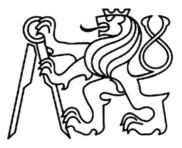
# Application of Magnetic Sensors for Navigation Systems

DOCTORAL THESIS

2007

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Czech Technical University in Prague Faculty of Electrical Engineering Department of Measurement



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