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Mario Hernán Castañeda García

**Design of Multiuser Multiantenna
Wireless Communication Systems**

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Technische Universität München

Design of Multiuser Multiantenna Wireless Communication Systems

Mario Hernán Castañeda García

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