

**Two Scale Multi-component and Multi-phase Model
for the Numerical Simulation
of Growth Processes in Saturated Porous Media
under Consideration of Bio-chemical Processes
- at the Example of the Human Liver**

von der Fakultät Architektur und Bauingenieurwesen
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M.Sc. Daniel Werner

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Vorsitz: Univ.-Prof. Dr.-Ing.habil. Achim Hettler

1. Gutachter: Univ.-Prof. Dr.-Ing. Tim Ricken

2. Gutachter: Univ.-Prof. Dr. med. Jan G. Hengstler

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Daniel Werner

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