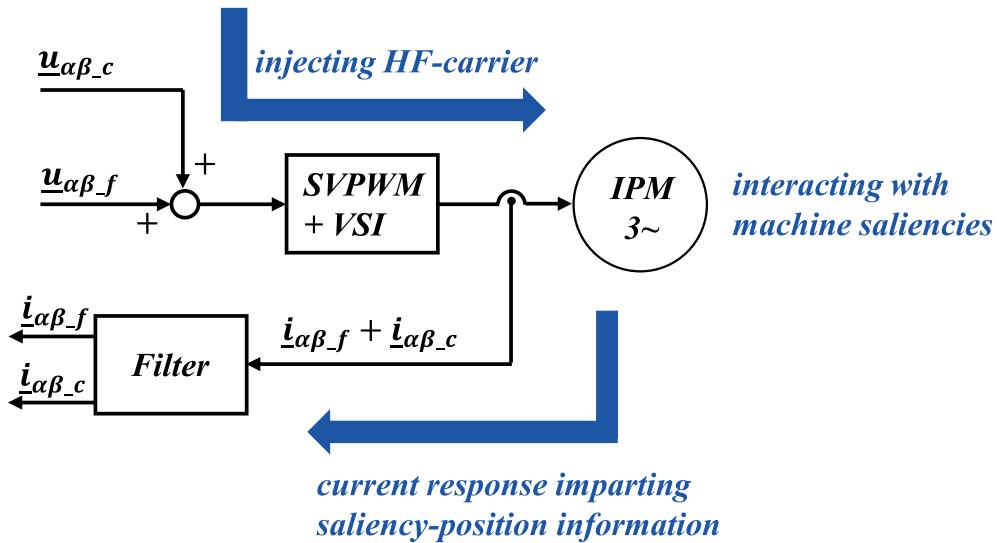


Forschungsberichte  
Elektrische Antriebstechnik und Aktorik

Hrsg.: Prof. Dr.-Ing. Dieter Gerling

Benjamin Grothmann

Online Detection and Compensation  
of Sensor-Faults in Electric Drives for  
Automotive Applications



# **Online Detection and Compensation of Sensor-Faults in Electric Drives for Automotive Applications**

**Benjamin Grothmann**

Vollständiger Abdruck der von der Fakultät für Elektro- und Informationstechnik der Universität der Bundeswehr München zur Erlangung des akademischen Grades eines

**Doktor-Ingenieurs (Dr.-Ing.)**

genehmigte Dissertation.

Prüfungsvorsitzender:

Prof. Dr. rer. nat. habil. Claus Hillermeier

Gutachter:

1. Prof. Dr.-Ing. Dieter Gerling

2. Prof. Robert D. Lorenz, Ph.D.

Die Dissertation wurde am 08.06.2018 bei der Universität der Bundeswehr München eingereicht und durch die Fakultät für Elektro- und Informationstechnik am 10.10.2018 angenommen. Die mündliche Prüfung fand am 29.11.2018 statt.



Forschungsberichte Elektrische Antriebstechnik und Aktorik

Band 37

**Benjamin Grothmann**

**Online Detection and Compensation of Sensor-Faults  
in Electric Drives for Automotive Applications**

Shaker Verlag  
Aachen 2019

**Bibliographic information published by the Deutsche Nationalbibliothek**

The Deutsche Nationalbibliothek lists this publication in the Deutsche Nationalbibliografie; detailed bibliographic data are available in the Internet at <http://dnb.d-nb.de>.

Zugl.: München, Univ. der Bundeswehr, Diss., 2018

Copyright Shaker Verlag 2019

All rights reserved. No part of this publication may be reproduced, stored in a retrieval system, or transmitted, in any form or by any means, electronic, mechanical, photocopying, recording or otherwise, without the prior permission of the publishers.

Printed in Germany.

ISBN 978-3-8440-6410-0

ISSN 1863-0707

Shaker Verlag GmbH • P.O. BOX 101818 • D-52018 Aachen

Phone: 0049/2407/9596-0 • Telefax: 0049/2407/9596-9

Internet: [www.shaker.de](http://www.shaker.de) • e-mail: [info@shaker.de](mailto:info@shaker.de)

*In memory of Franz Wallner.  
Your life and friendship will be my inspiration - forever.*



---

# Abstract

Torque production in servo drives is directly linked to current vector control and thus relying on accurate state-feedback from the sensing devices. Distortion of these signals in case of fault-occurrence in the sensors can lead to unwanted control system response. In worst-case, instability or physical damage of the system might force a shutdown of the drive. This is not tolerable especially for safety-relevant drives in automotive applications. In this thesis, methods for online detection and compensation of sensor faults for interior permanent magnet machine (IPM)-drives are developed. Position sensor outage, as well as current sensor gain faults including the case of current sensor outage, are addressed. Model-based methodologies are developed, allowing for fault-detection and fault-compensation without the requirement of auxiliary hardware alongside the already existing devices. Practical testings are conducted on a general-purpose IPM-drive representing an automotive application. Self-sensing is applied in parallel to the current regulation, using the estimated position to monitor the position transducer. Saliency-tracking self-sensing is applied for low speed-ranges, whereas back-EMF (BEMF)-based self-sensing is used for intermediate and higher speeds. Suitable transitioning between both techniques is chosen, to allow for position estimation over the complete speed operating-range. A fault-compensation framework is presented, using a weighting function to replace the faulty sensor signal with the estimated position for state-feedback, after detection of a position sensor fault. This framework is shown to achieve fast and smooth reaction to position sensor outage. Practical implementation caveats regarding self-sensing feasibility and estimation accuracy are discussed thoroughly. Based on the magnetic identification of the given drive, metrics for early assessment of self-sensing applicability are derived. Conducted testings show reliable fault-compensation for any speed operating-range. Limiting aspects identified are steep transients in commanded current and an overall physical restricton of the given implementation to current loadings below 50 % of the specified current operating-range, at low speeds. For the compensation of current sensor gain faults, adaptive methodologies based on the deterministic response to high frequency injection (HFI) are investigated. An existing gain re-balancing scheme is optimized for fast and accurate fault-compensation. In combination with a novel direct phase gain re-balancing (DGB)-technique, the resulting gain fault-compensation framework is shown to potentially operate reliably for the complete speed operating-range. Limitations of the DGB-method regarding the calculation of reference values for the adaptive loops are discussed in detail. The DGB-technique is also proposed as suitable current sensor outage detection. Outage of one or both current sensors is then captured by enhancing the proposed compensation framework with a closed-loop observer based current vector reconstruction known from literature. Thus, the complete range of current sensor gain faults is covered. Each method for fault-compensation discussed in this thesis is assessed based on a predefined set of requirements, concluding in aspects and potentials for future optimizations.

## Kurzfassung

Die Drehmomenterzeugung in Servoantrieben steht in direktem Zusammenhang mit der Regelung des Stromvektors und basiert daher auf der akuraten Bereitstellung der Ist-Werte durch die Sensorik. Abweichungen dieser Signale durch das Auftreten von Sensorfehlern können zu unerwünschten Systemantworten der Regelung führen. Im schlimmsten Falle erzwingen Instabilität oder physikalische Beschädigung des Systems ein Abschalten des Antriebs. Dies ist insbesondere für sicherheitsrelevante Antriebe in Automobilanwendungen nicht zu tolerieren. In der vorliegenden Dissertation werden Methoden zur Echtzeit-Diagnose und -Kompensation von Sensorfehlern für Antriebe mit Permanentmagnet Synchronmaschinen mit vergraben Magneten (IPM) entwickelt. Im Blickpunkt stehen dabei der Ausfall des Lagegebers, sowie Skalierungsfehler in den Stromsensoren inklusive Stromsensorsausfall. Es werden modellbasierte Methoden entwickelt, welche die Fehlerdiagnose und Fehlerkompensation ohne Hinzunahme weiterer Hardware zu den bereits verwendeten Sensoren ermöglichen. Praktische Tests werden an einem Standard-IPM-Antrieb in Anlehnung an Automobilanwendungen durchgeführt. Eine lagegeberlose Regelung (Self-Sensing) ist parallel zur Stromregelung implementiert und der geschätzte Winkel wird zur Überwachung des Lagegebers verwendet. Für kleine Drehzahlen wird ein Anisotropie-basiertes Verfahren zur lagegeberlosen Regelung verwendet, während für mittlere bis zu hohen Drehzahlbereichen ein Verfahren basierend auf der induzierten Spannung genutzt wird. Um die Rotorlage über den gesamten Drehzahlbereich schätzen zu können wird eine geeignete Übergangsfunktion zwischen beiden Verfahren gewählt. Ein Schema zur Fehlerkompensation wird vorgestellt, welches eine Gewichtsfunktion zum Ersetzen des fehlerhaften Sensorsignals mit der geschätzten Rotorlage als Ist-Wert nach Eintreten eines Lagegeberfehlers verwendet. Es wird gezeigt, dass diese Struktur eine schnelle und sanfte Kompensation bei Ausfall des Lagegebers ermöglicht. Praktische Problemstellungen bei der Implementierung der lagegeberlosen Regelung werden detailliert diskutiert. Basierend auf der Identifikation magnetischer Systemparameter des verwendeten Antriebs werden Richtlinien zur frühen Bewertung der Umsetzbarkeit lagegeberloser Regelungen hergeleitet. Die durchgeföhrten Tests zeigen zuverlässige Fehlerkompensation für den kompletten Drehzahlbereich. Als limitierende Aspekte werden steile Transienten in den Strom-Sollwerten festgestellt, als auch eine physikalische Beschränkung der Anwendung auf Stromarbeitspunkte kleiner 50 % des spezifizierten Stromarbeitsbereichs für kleine Drehzahlen. Zur Kompensation von Skalierungsfehlern in der Stromsensorik werden adaptive Methoden basierend auf der deterministischen Systemantwort auf Hochfrequenz-Signalinjektion (HFI) untersucht. Eine bereits existierende Methode zum Neuabgleich von Skalierungsfehlern wird zur schnellen und akuraten Fehlerkompensation optimiert. Es wird gezeigt, dass das resultierende Konzept zur Kompensation von Skalierungsfehlern in Kombination mit einem neuartigen Verfahren zum direkten Neuabgleich der Sensorskalierungen (DGB) potentiell über dem gesamten Drehzahl-Arbeitsbereich verlässlich anwendbar ist. Limitierungen der DGB-

Methode bezüglich Berechnung von Ist-Werten ihrer adaptiven Regelschleifen werden detailliert behandelt. Die DGB-Methode wird darüber hinaus als geeignetes Verfahren zur Erkennung eines Stromsensorsausfalls angedacht. Der Ausfall von einem oder beider Stromsensoren wird daraufhin durch Erweiterung des Konzepts zur Fehlerkompensation durch einen aus der Literatur bekannten Beobachter zur Rekonstruktion des Stromvektors abgefangen. Somit ist die komplette Bandbreite an Stromsensorskalierungsfehlern abgedeckt. Jedes in der vorliegenden Dissertation zur Fehlerkompensation diskutierte Verfahren wird anhand vordefinierter Anforderungskriterien bewertet, was schließlich in Aspekten und Potentialen für künftige Optimierungsansätze mündet.

## Acknowledgements

First, I want to thank Prof. Dr.-Ing. Dieter Gerling for offering me this great research project, as well as the constant support and overall supervision. I am very grateful for all of his advice and motivation provided during my work. I also want to thank Prof. Robert D. Lorenz, Ph.D., for being second supervisor for this thesis and giving me the opportunity to spend a exceptionally instructive time as visiting scholar at the Wisconsin Electric Machines and Power Electronics Consortium (WEMPEC) in Madison.

At this point, many thanks go out to Marc Petit, Huthaifa Flieh, Tim Slininger, Gene Rush, Muhammad Alvi, Dan Erato and the rest of the WEMPEC-family. All the discussions and time spent together was not only fun, but also an honor and a privilege I cannot emphasize enough.

I want to thank former internship and masters-degree students at AUDI, Katharina Wiesbeck, Dennis Jagosz, Jürgen Rieblinger, Kai Taylor, Divahar Mani and Andreas Rauscher. Their talent, enthusiasm and dedication was an enrichment for the project. Further thanks also go out to Wolfgang Brandstätter, Frank Lachnit, Christine Schmidt, Christoph Raith and the rest of the AUDI R&D department for the great and always fun time.

From all of my former colleagues from the chair of electrical drives and actuators, Universität der Bundeswehr München, I want to greatly emphasize my gratitude to Michael Saur, Bastian Lehner and Niko Reiland, for their unconditional support during this thesis. In my time in Munich I was able to work together closely with Michael Saur, from which my personal development, as well as my professional career still benefit on a great scale. Special thanks also to Basti Lehner, for his always open ear, fruitful discussions and all the fun times spent together. Many, many thanks then go out to Niko Reiland, for his amazing support facing the rocky roads in our projects, including his role as a constant reminder of what day of the week it is.

Regarding my friends and supporters from Regensburg, I want to greatly thank my former professors Prof. Bernhard Hopfensperger and Prof. Dieter Seifert, for advice and support during my Masters-degree and up to this day. Thank you Andi Neumeier and Michl Forster for not only being close friends ever since we started our studies together, but also for acting as mentors during tough decisions.

I am very, very grateful for the long list of my friends from my hometown, especially Robert, Sabrina, Patrick, Tanja, Anton, Karin, Caro, Martin, Benedikt, Steffi, Manfred, Christine, Daniel and Katharina, for their support and suffering all the hard times during this project, reminding me of where my heart can always find a place to call home.

These last lines I saved for thanking my parents, Franziska and Nik. Without you, I would never be at where I am right now.

# Contents

<b>Abstract</b>	<b>i</b>
<b>Kurzfassung</b>	<b>ii</b>
<b>Acknowledgements</b>	<b>iv</b>
<b>List of Figures</b>	<b>viii</b>
<b>List of Tables</b>	<b>xiii</b>
<b>Nomenclature</b>	<b>xiv</b>
<b>1 Introduction</b>	<b>1</b>
1.1 Project Overview and Requirements . . . . .	1
1.1.1 Drive Systems for Automotive Applications . . . . .	2
1.1.2 Electric Machine Drive Faults under Consideration . . . . .	2
1.1.3 Requirements for Fault-Detection and Fault-Compensation . . . . .	3
1.2 Thesis Outline . . . . .	5
<b>2 State-of-the-Art Review</b>	<b>6</b>
2.1 Permanent-Magnet AC Machine Modeling . . . . .	6
2.1.1 dq Modeling . . . . .	7
2.1.2 Enhanced Machine Modeling including Saturation . . . . .	12
2.2 Magnetic Model Identification . . . . .	13
2.2.1 Differential Inductances . . . . .	14
2.2.2 Flux Linkages . . . . .	15
2.3 Vector Control System Design . . . . .	18
2.3.1 Torque Production Principles . . . . .	19
2.3.2 PI Current Regulation . . . . .	20
2.3.3 Enhanced Control Systems using State Observers . . . . .	23
2.4 Self-Sensing for PM Synchronous Machines . . . . .	28
2.4.1 Saliency-Tracking Self-Sensing . . . . .	29
2.4.2 BEMF-based Self-Sensing . . . . .	32
2.4.3 Filter-Techniques . . . . .	33
2.4.4 Transitioning between Self-Sensing Methods . . . . .	37
2.5 Sensor Fault-Detection and Fault-Mitigation . . . . .	37
2.5.1 Current Sensing . . . . .	38
2.5.2 Position Sensing . . . . .	41
2.6 Research Opportunities . . . . .	42

<b>3 Baseline Control System Implementation</b>	<b>44</b>
3.1 Testbench Setup for Control Prototyping . . . . .	44
3.1.1 Overview . . . . .	44
3.1.2 Standard Current Vector Control Design and Implementation . . . . .	46
3.1.3 HFI-Signal Design Considerations . . . . .	49
3.1.4 Summary of Data-Sheet and Tuning Parameters . . . . .	51
3.2 Automated Magnetic Model Identification . . . . .	52
3.2.1 Constant Speed Identification of Flux-Linkages . . . . .	52
3.2.2 Zero Speed Identification of Differential Inductances . . . . .	55
3.3 Conclusions . . . . .	58
<b>4 Rotor Position Sensor Fault-Detection and Fault-Compensation</b>	<b>59</b>
4.1 Conceptual Approach . . . . .	60
4.2 Position Information contained in Physical Machine Properties . . . . .	61
4.2.1 Saliency Position Modulation of HFI-Response . . . . .	61
4.2.2 Experimental Feasibility-Assessment of Saliency-Tracking based Self-Sensing . . . . .	69
4.2.3 Rotor-Flux Vector Position in BEMF . . . . .	74
4.3 Saliency-Tracking Self-Sensing for Low Speed-Range . . . . .	75
4.3.1 Implementation Overview . . . . .	75
4.3.2 Identified Feasibility Range . . . . .	79
4.3.3 Steady-State Accuracy . . . . .	80
4.3.4 Transient-State Accuracy . . . . .	85
4.3.5 Recommended Metrics for Choosing a Filter-Strategy . . . . .	87
4.4 Back-EMF-Tracking Self-Sensing for Intermediate and High Speed-Range	93
4.4.1 Implementation Overview . . . . .	93
4.4.2 Identified Feasibility Range . . . . .	95
4.4.3 Steady-State Accuracy . . . . .	95
4.4.4 Transient-State Accuracy . . . . .	96
4.5 Transitioning between Speed-Ranges . . . . .	100
4.5.1 Implementation Overview . . . . .	100
4.5.2 Performance Evaluation . . . . .	101
4.6 Framework for Fault-Compensation . . . . .	104
4.6.1 Implementation Overview . . . . .	104
4.6.2 Fault-Compensation Performance . . . . .	104
4.7 Conclusions . . . . .	107
<b>5 Current Sensor Fault-Detection and Fault-Compensation</b>	<b>109</b>
5.1 Conceptual Approach . . . . .	109
5.2 Current Sensor State Information contained in HFI-Response . . . . .	110
5.2.1 General Gain-Fault Model for a reduced Set of Sensors . . . . .	111
5.2.2 HFI-Response Analysis in Presence of Gain-Faults . . . . .	112
5.3 Sequence-based Gain Re-Balancing (SGB) . . . . .	114
5.3.1 System Overview . . . . .	114
5.3.2 Practical Implementation . . . . .	117
5.3.3 Identified Feasibility Range . . . . .	118
5.3.4 No-Fault Operation . . . . .	118
5.3.5 Fault-Compensation Performance . . . . .	118

5.4	Novel Direct Phase-Gain Re-Balancing (DGB) for Low Speeds including Standstill . . . . .	125
5.4.1	System Overview . . . . .	125
5.4.2	Practical Implementation . . . . .	126
5.4.3	Identified Feasibility Range . . . . .	129
5.4.4	No-Fault Operation . . . . .	130
5.4.5	Fault-Compensation Performance . . . . .	131
5.5	Fault-Compensation Potentials for complete Fault- and Operating-Range .	136
5.5.1	Combination of SGB and DGB for Gain Fault-Compensation for full Speed-Range . . . . .	136
5.5.2	Enhancement for Compensation of Sensor Outage . . . . .	139
5.6	Conclusions . . . . .	142
<b>6</b>	<b>Conclusions</b>	<b>144</b>
6.1	Assessment of the Fault-Compensation Methods with Respect to the Requirements . . . . .	144
6.1.1	Position Sensor Fault-Detection and Fault-Compensation . . . . .	145
6.1.2	Current Sensor Fault-Detection and Fault-Compensation . . . . .	147
6.2	Contributions . . . . .	149
6.3	Future Work Recommendations . . . . .	150
<b>References</b>		<b>153</b>

# List of Figures

1.1	Conceptual overview of the sensor faults addressed by this research in context of a general-purpose vector controlled IPM drive . . . . .	2
2.1	Spatial orientation of the synchronously rotating $dq$ reference frame (2-pole IPM machine assumption). Left: Complex plane; Middle: $dq$ frame attached to PM rotor; Right: Spatial deflection of the $dq$ frame "coils" with respect to the stationary $\alpha\beta$ frame . . . . .	7
2.2	State block diagram of the complex vector model (2.12) . . . . .	9
2.3	State block diagram of the electric system of an IPM in complex component format . . . . .	10
2.4	Typical experimental setup for general purpose magnetic model identification [17] . . . . .	14
2.5	Exemplary current trajectories for automated differential inductance identification from [20] . . . . .	15
2.6	Experimentally identified differential inductances using AC current injection, reported in [26] . . . . .	16
2.7	Reported experimental magnetic model identification for an IPM, with and without load-drive, to calculate the operating-point dependent flux linkages . . . . .	17
2.8	Automated constant speed identification from [16] for a highly utilized synchronous reluctance machine drive . . . . .	18
2.9	State block diagram of the simplified mechanical system . . . . .	20
2.10	Schematic of a standard synchronous frame PI current regulator for a simplified machine model (RL-load), [10] . . . . .	20
2.11	Analysis of speed-dependent zero-pole cancellation inaccuracy for synchronous frame PI current regulators from the early publication of [9] .	21
2.12	Complex vector current controller for an IPM, [10] . . . . .	22
2.13	Comparison between the different current regulators, [10] . . . . .	22
2.14	General open-loop and closed-loop format observers . . . . .	24
2.15	Luenberger-Style motion observer for motion state estimation . . . . .	25
2.16	Luenberger-Style current observer in vector format representation for SPM drives (BEMF-voltage assumed to be decoupled) . . . . .	26
2.17	General vector-tracking observer . . . . .	27
2.18	Simplified schematic of the resolver-to-digital principle . . . . .	29
2.19	Basic HFI concept from an early publication [43] . . . . .	30
2.20	Saliency-tracking observer models . . . . .	30
2.21	Exemplary saliency images of an IPM drive for different current operating-points, [51] . . . . .	31

---

2.22	Saliency-tracking using alternating injection-signals for HFI . . . . .	32
2.23	Related model-based concepts for rotor position estimation based on BEMF . . . . .	33
2.24	Basic formats for synchronous reference frame filters . . . . .	34
2.25	Fundamental current observer embedded in the signal-processing related to self-sensing for an induction machine drive, [81] . . . . .	36
2.26	Schematical implementation-examples of the Goertzel Algorithm . . . . .	36
2.27	Usage of image processing to replace bandwidth-limited filtering in heterodyning, [88] . . . . .	37
2.28	Weighting function for speed-dependent transitioning between rotor position estimation models, [65] . . . . .	37
2.29	Analysis and compensation of steady-state speed-ripple produced due to scaling-faults and offset-faults (Top: Rotor velocity; Bottom: Frequency analysis of the speed error), [91] . . . . .	38
2.30	Online current sensor fault-compensation concept as reported in [93] . . . . .	39
2.31	Adaptive current sensor gain re-balancing based on HFI, [90] . . . . .	40
2.32	Fundamental current observer including a sensor gain matrix for current vector reconstruction, [97] . . . . .	41
2.33	Experimental fault-detection and fault-compensation sequence for an encoder fault, presented in [97] . . . . .	42
3.1	Current control system design assumption in complex vector format using a simplified machine model . . . . .	47
3.2	Command-tracking response of the implemented vector control to a $i_q^*$ -step-command from 0 A to 50 A at different speed operating-points; Attempted control-bandwidth $f_{BW} = 300$ Hz . . . . .	49
3.3	Current vector control system including HFI superimposed on fundamental operation . . . . .	50
3.4	Open-loop HFI-response currents at standstill, no load ( $U_c = 1$ V, $f_c = 1$ kHz) . . . . .	51
3.5	Schematic example for the identification of a specific point in the flux-maps using motoring/generating operation . . . . .	54
3.6	Resulting flux linkage maps using constant speed identification, $n = 300$ rpm, 5 A current-resolution, 0.25 s time per operating-point . . . . .	54
3.7	Exemplary current-traces of the automated zero speed identification sequence . . . . .	56
3.8	Resulting differential inductance maps using the zero speed current-injection identification ( $f_{AC} = 600$ Hz, $I_{HF} = 1$ A), averaged over one electric period spatially ( $72^\circ$ deg.mech.) . . . . .	57
4.1	Parallel approach of position sensor fault-detection and fault-compensation implementation using self-sensing . . . . .	61
4.2	CVFFT of the current response to HFI . . . . .	65
4.3	Geometrical representation of additional shift in magnitude and phase of the negative sequence current vector due to cross-saturation . . . . .	67
4.4	CVFFT of the current response to HFI ( $U_c = 1$ V, $f_c = 1$ kHz, $n = 6$ rpm) for different current vectors ( $i_d^*, i_q^*$ ) . . . . .	69
4.5	Experimental identification of negative sequence magnitude $I_{cn}$ for Metric #1 . . . . .	72

---

4.6	Calculated saliency images for 8 rotor revolutions based on the spectra obtained from Fig. 4.4a (a) and Fig. 4.4c (b), for Metric #2 . . . . .	73
4.7	State block diagram of the voltage model of an SPM in the stationary reference frame formulated to provide the flux linkage vector imparting the rotor position . . . . .	75
4.8	Overall scheme for HFI-based self-sensing implementation for motion state estimation, in context of fault-detection and fault-compensation, as well as the transitioning to BEMF-based self-sensing . . . . .	75
4.9	SRFF with embedded closed-loop fundamental current observer . . . . .	77
4.10	Schematic overview of the implemented saliency-tracking observer . . . . .	78
4.11	Experimental tracking-loss approaching a current operating-point of $i_q^* = 55$ A (@ 30 rpm) . . . . .	80
4.12	Experimental evaluation of the available motion state estimates (steady-state, 30 rpm, 30 A, $\Delta\hat{\theta} = 15^\circ$ ) . . . . .	81
4.13	Comparison of angular errors and velocity estimation for different current loading operating-points (steady-state, 30 rpm, $\Delta\hat{\theta} = 11^\circ$ ) . . . . .	83
4.14	Comparison of angular errors and velocity estimation for different speed operating-points (steady-state, 20 A) . . . . .	84
4.15	Evaluation of motion state estimation during transient-state operation by either step-changes in current (vector control) or speed (load-drive), $\Delta\hat{\theta} = 11^\circ$ . . . . .	86
4.16	Subtraction-based SRFF . . . . .	88
4.17	Resulting saliency images for different current-loading operating-points (steady-state, 60 rpm); Top: SSRFF; Bottom: Cascaded SRFF imparting the fundamental current observer . . . . .	89
4.18	Filter comparison regarding transient-state estimation dynamics, applying a current-step (marked by black lines) from 10 A to 20 A (constant speed of 30 rpm) . . . . .	91
4.19	Filter comparison regarding the dynamic distortion in the negative sequence reference frame due to current-steps (steps marked by black lines, constant speed of 60 rpm, no HFI applied); Top: Cascaded SRFF imparting the fundamental current observer; Bottom: SSRFF . . . . .	92
4.20	BEMF-estimator for rotor position estimation, based on voltage model and a recursive gain-stage . . . . .	93
4.21	Overall scheme for BEMF-based self-sensing implementation for motion state estimation, in context of fault-detection and fault-compensation . . . . .	94
4.22	Experimental feasibility assessment of the implemented BEMF-based self-sensing scheme (step-change in commanded speed from 50 rpm to 100 rpm, constant current 10 A) . . . . .	96
4.23	Comparison of angular errors and velocity estimation using BEMF-tracking for different steady-state operating-points of rotor speed ( $n$ ) and current-loading ( $i_q$ ), $\Delta\hat{\theta} = 0^\circ$ ; Top: Estimated angles vs. measured angle; Middle: Estimation errors with respect to mean error; Bottom: Estimated angular velocities . . . . .	97
4.24	Comparison of angular errors and velocity estimation using BEMF-tracking during current and speed transients ( $\Delta\hat{\theta} = 0^\circ$ ); Top: estimation error; Middle: Angular velocity estimates; Bottom: Respective command trajectories . . . . .	99

---

4.25	Blending of the two self-sensing techniques using weighted transitioning and a unified tracking observer for motion state estimation . . . . .	101
4.26	Dynamic performance evaluation of the implemented blending framework; Top: Estimation errors; Second row: Blending variable from weighting; Third row: Estimated angular velocities; Bottom: Respective command trajectories . . . . .	103
4.27	Weighted position sensor fault-compensation framework . . . . .	104
4.28	Experimental evaluation of the proposed fault-compensation framework by unplugging the physical transducer (denoted by black line) . . . . .	106
5.1	Adaptive approach of current sensor gain fault-detection and fault-compensation implementation . . . . .	110
5.2	Measured current vector spectrum before and after a gain-fault of $k_A = 1.5$ (operating-point: $n = 600$ rpm, $i_q^* = 10$ A) . . . . .	113
5.3	Online gain re-balancing methodology as presented in [90] . . . . .	115
5.4	Simplified spectral separation of the HFI-response current vector sequences in the stationary reference frame in case of gain-deviation for non-zero speed	116
5.5	Overview of the sequence-based adaptive current sensor-gain re-balancing methodology for IPM drives . . . . .	116
5.6	Measured positive sequence magnitudes as a function of speed and current-loading operating-conditions [4] . . . . .	117
5.7	Exemplary gain fault-compensation performance results ( $k_A = 2$ , fault-instant marked by black lines) for low-speed operating points @ $i_q = 70$ A, $K_i = 8$ . Top row: physical phase currents. Bottom row: compensation gains . . . . .	119
5.8	Investigation of the no-fault impact for different operating-conditions ( $K_i = 2$ ). Top row: compensation gains. Middle row: physical currents in $dq$ frame. Bottom row: operating-speed . . . . .	119
5.9	Exemplary fault-compensation investigation during steady-state operation with a fault-injection of $k_A = 2$ (fault-instant marked by black line) for two different $K_i$ -tunings. Top row: physical phase currents. Middle row: physical currents in $dq$ frame. Bottom row: compensation gains . . . . .	121
5.10	Fault-compensation for an experiment of successive fault-occurrence in both sensor gains (marked by black lines), steady-state operation (50 A, 300 rpm, $K_i = 8$ ). Top row: physical phase currents. Middle row: physical currents in $dq$ frame. Bottom row: compensation gains . . . . .	122
5.11	Experimental results for fault-occurrence of $k_A = 2$ (marked by black lines) during transient operation ( $K_i = 2$ ). Top: current-transient from 30 A to 70 A, @1000 rpm; Bottom: speed-transient from 200 rpm to 1000 rpm, @70 A . . . . .	123
5.12	Experimental investigation of fail-operational performance of the SGB-method considering a double-fault (marked by black lines, $K_i = 8$ ); Top: re-balancing gains; Middle: physical currents translated into $dq$ frame; Bottom: operating-speed set by the load-drive . . . . .	124
5.13	Overview of the proposed direct phase-gain re-balancing methodology, [101] . . . . .	125
5.14	Cascaded SRFF-based filtering topology for extracting the HF phase currents, [101] . . . . .	126

5.15	DGB-method compensation controller state block diagrams . . . . .	129
5.16	Measured vs. precalculated HFI phase current magnitudes for different operating-speeds (40 A), adaptive compensation deactivated; Top: phase $A$ ; Bottom: phase $B$ . . . . .	130
5.17	No-fault evaluation of the DGB-method for different operating-conditions ( $K_i = 2$ ); Top: re-balancing gains; Middle: physical currents translated into $dq$ frame; Bottom: operating-speeds set by the load-drive . . . . .	131
5.18	Investigation of fault-compensation performance of the proposed DGB-method for different operating-points ( $K_i = 2$ ), for a fault $k_A = 2$ (marked by black line); Top: physical currents translated into $dq$ frame; Middle: re-balancing gains; Bottom: comparison of calculated and measured HFI-response magnitudes for phase $A$ . . . . .	133
5.19	Investigation of fault-compensation performance of the proposed DGB-method in case of a double fault (faults marked by black lines each, $K_i = 2$ , operating-point: 35 A, 0 rpm); Top row: physical currents translated into $dq$ frame; Second row: re-balancing gains; Third row: comparison of calculated and measured HFI-response magnitudes for phase $A$ ; Bottom row: comparison of calculated and measured HFI-response magnitudes for phase $B$ . . . . .	134
5.20	Fail-operational testing scenario for the DGB-method ( $K_i = 2$ ), including transients in current-loading and speed [101] . . . . .	135
5.21	Schematical combination of the SGB- and DGB-methods, using a simple software-switch for transitioning between speed-ranges . . . . .	137
5.22	Experimental results for the transition in gain fault-compensation merging DGB and SGB ( $K_i = 8$ ) for a double fault (first: $k_A = 2$ , second: $k_B = 2$ , indicated by black lines) and speed-trajectory . . . . .	138
5.23	Conceptual implementation of the current sensor outage compensation . .	140
5.24	Experimental evaluation of combining the DGB-method with sensor outage compensation, decreasing gain $A$ from $k_A = 0.5$ (already compensated) until the outage-threshold is reached for initiating the outage compensation (operating-point 200 rpm, 30 A) . . . . .	141

# List of Tables

3.1	Relevant settings specified regarding practical implementation . . . . .	52
4.1	Available signals from cascading tracking observer and a motion observer	79
4.2	Relevant settings regarding HFI-based self-sensing implementation . . . .	79
4.3	Available signals from cascading BEMF-estimator, vector tracking and a motion observer . . . . .	94
4.4	Relevant settings regarding BEMF-based self-sensing implementation . .	95

# Nomenclature

## List of Abbreviations

AC	alternating current
BW	bandwidth
BEMF	back electromotive force
CL	closed-loop
CO	current observer
CVC	complex vector current regulator
CVFFT	complex vector fast Fourier transform
DC	direct current
DGB	direct phase-gain re-balancing
FFT	fast Fourier transform
FSCW	fractional slot concentrated windings
HF	high frequency
HFI	high frequency injection
IPM	interior permanent magnet synchronous machine
MIMO	multiple-input multiple-output
MO	motion observer
MTPA	maximum torque per ampere
OP	operating-point
PI	proportional integral
PID	proportional integral differential
PM	permanent magnet
SDFT	sliding discrete Fourier transform
SFb	state-feedback
SGB	sequence-based gain re-balancing
SISO	single-input single-output
SNR	signal-to-noise ratio
SPM	surface mounted permanent magnet synchronous machine
SRFF	synchronous reference frame filter
SSRFF	subtraction-based synchronous reference frame filter
SVPWM	space vector pulse width modulation
TO	tracking observer
VSI	voltage source inverter

## List of Symbols

### General Notation

$u$	stator voltage
$i$	stator current
$\psi$	flux linkage
$\omega$	angular velocity
$\theta$	rotor position
$L$	inductance
$j$	complex number
$A, B, C$	three phase notation
$x_A, x_B, x_C$	three phase ( $ABC$ ) quantity $x$
$\underline{x}_{dq} = x_d + jx_q$	complex vector $x$ in rotary ( $dq$ ) reference frame
$x_d, x_q$	complex components in rotary ( $dq$ ) reference frame
$\underline{x}_{\alpha\beta} = x_\alpha + jx_\beta$	complex vector $x$ in stationary ( $\alpha\beta$ ) reference frame
$x_\alpha, x_\beta$	complex components in stationary ( $\alpha\beta$ ) reference frame
$X$	magnitude of signal $x$
$\underline{x}$	scalar state vector
$\mathbf{X}$	scalar matrix
$\hat{x}$	estimate of $x$
$x^*$	command/reference of $x$
$\dot{x}$	derivative of $x$
$x_c$	carrier signal $x$
$x[k]$	quantity $x$ sampled at $k$ -th sample instant
$\mathbf{X}^{-1}$	matrix inverse of $\mathbf{X}$
$\underline{x}^\dagger$	complex conjugate of complex vector $\underline{x}$

### Special Symbols

$A_1, A_2$	generic identifiers
$\mathbf{A}$	generic system matrix
$B_1, B_2$	generic identifiers
$\mathbf{B}$	generic input matrix
$b$	active damping controller gain
$\mathbf{C}$	generic output matrix
$D$	generic disturbance
$\varepsilon$	error signal
$\varepsilon_{pc}, \varepsilon_{cp}$	error signals in SGB method created from positive sequence
$\varepsilon_{nc}, \varepsilon_{cn}$	error signals in SGB method created from negative sequence
$\varepsilon_A, \varepsilon_B$	error signals in DGB method created from respective phase gain errors
$\varepsilon i_{\alpha\beta}, \varepsilon i_{dq}, \Delta i_{dq}$	current vector deviations
$e_{PM}$	BEMF voltage
$\epsilon f$	set of eigenvalues

---

$\underline{e}_{\alpha\beta}$	BEMF voltage vector in stationary ( $\alpha\beta$ ) reference frame
$\gamma$	relative difference saliency ratio
$f_c$	carrier frequency in [Hz]
$f_i$	generic injection frequency in [Hz]
$f_r$	excitation frequency in [Hz]
$f_s$	sampling/switching frequency in [Hz]
$f_{BW}$	bandwidth in [Hz]
$f_{AC}$	identification test signal frequency in [Hz]
$G_{CL}$	closed-loop transfer function
$G_{dq}$	transfer function of a system in $dq$ vector notation
$G_o$	open-loop transfer function
$G_{PI}$	proportional integral controller transfer function
$G(\theta_r)$	sensor gain matrix for current reconstruction
$h$	harmonic number
$i_{Ac}, i_{Bc}, i_{Cc}$	three phase carrier current responses to HFI
$i_{Am}, i_{Bm}$	measured phase currents scaled by sensor gains
$i_{qc}$	quadrature carrier current vector component in estimated $dq$ reference frame
$\underline{i}_{\alpha\beta\_f}$	fundamental current vector in stationary ( $\alpha\beta$ ) reference frame
$\underline{i}_{dq,AC} = i_{d,AC} + j i_{q,AC}$	alternating test signal current vector in rotary ( $dq$ ) reference frame
$\underline{i}_{dq,DC} = i_{d,DC} + j i_{q,DC}$	static operating point current vector in rotary ( $dq$ ) reference frame
$\underline{i}_{dq,HF}$	injection current vector in rotary ( $dq$ ) reference frame
$\underline{i}_{dq\_f}$	fundamental current vector in rotary ( $dq$ ) reference frame
$\underline{i}_{\alpha\beta\_c} = i_{\alpha\_c} + j i_{\beta\_c}$	carrier current response to HFI
$\underline{i}_{\alpha\beta cm} = i_{\alpha cm} + j i_{\beta cm}$	measured carrier current response to HFI scaled by sensor gains
$\underline{i}_{\alpha\beta\_cn} = i_{\alpha\_cn} + j i_{\beta\_cn}$	negative sequence carrier current response to HFI
$\underline{i}_{\alpha\beta\_cp}$	positive sequence carrier current response to HFI
$\underline{i}_n$	generic current vector associated with a negative sequence
$\underline{i}_p$	generic current vector associated with a positive sequence
$\underline{i}_{dq,M} = i_{d,M} + j i_{q,M}$	current vector in rotary ( $dq$ ) reference frame for motoring operation
$\underline{i}_{dq,G} = i_{d,G} + j i_{q,G}$	current vector in rotary ( $dq$ ) reference frame for generating/breaking operation
$\underline{i}_{dqs\_cn}^{cn}$	negative sequence vector isolated in its negative sequence reference frame
$I_c$	positive sequence carrier current vector magnitude (SPM)
$I_{cn}$	negative sequence carrier current vector magnitude

---

$I_{cp}$	positive sequence carrier current vector magnitude
$I_{cn\_cs}$	negative sequence carrier current vector magnitude through of cross-saturation
$I_{cns}$	resulting negative sequence carrier current vector magnitude including cross-saturation
$I_{cn\_h}$	multiple saliency vector magnitude
$I_{max}$	specified maximum current
$J$	rotor inertia
$K$	generic identifier
$k_A, k_B$	phase current sensor gains
$\Delta k$	difference gain
$\Sigma k$	mean gain
$K_{AB}$	sensor phase gain matrix
$K_{\alpha\beta}$	sensor gain matrix transformed into stationary ( $\alpha\beta$ ) reference frame
$K_p, K_P, K_{Pd}, K_{Pq}, r_o$	proportional controller gain stages
$K_i, K_{iA}, K_{iB}, K_I, r_{io}$	integral controller gain stages
$K_{err}$	weighting factor
$K$	active stiffness controller gain
$K_M$	mean error correction factor (SGB method)
$K_R$	relative error correction factor (SGB method)
$K_A, K_B$	phase error correction factors (DGB method)
$L_d, L_q$	apparent direct and quadrature (self-) inductance
$M_{dq}, M_{qd}$	apparent mutual inductances
$L_{dq}$	unified inductance substitute
$L_{dq}$	apparent inductance matrix in rotary ( $dq$ ) reference frame
$L_{\alpha\beta}$	apparent inductance matrix in stationary ( $\alpha\beta$ ) reference frame
$l_{dq}$	differential inductance matrix in rotary ( $dq$ ) reference frame
$l_{\alpha\beta}$	differential inductance matrix in stationary ( $\alpha\beta$ ) reference frame
$L_s$	synchronous inductance
$\Delta L$	difference inductance (in terms of apparent inductances)
$\Delta l$	difference inductance (in terms of differential inductances)
$\Sigma L$	average inductance (in terms of apparent inductances)
$\Sigma l$	average inductance (in terms of differential inductances)
$l_{dd}, l_{qq}$	direct and quadrature differential (self-) inductance
$l_{dq}, l_{qd}$	differential mutual inductances
$n$	rotor speed
$n_{max}$	specified maximum rotor speed

---

$\varphi_h$	phase shift with respect to harmonic $h$
$p$	number of pole pairs
$\psi_{PM}$	rotor flux linkage
$\underline{\psi}_{\alpha\beta,BEMF}$	rotor flux linkage vector in stationary ( $\alpha\beta$ ) reference frame
$\underline{\psi}_{dq,M} = \psi_{d,M} + j\psi_{q,M}$	flux linkage vector in rotary ( $dq$ ) reference frame for motoring operation
$\underline{\psi}_{dq,G} = \psi_{d,G} + j\psi_{q,G}$	flux linkage vector in rotary ( $dq$ ) reference frame for generating/breaking operation
$R$	ohmic resistance
$r_V$	virtual resistance
$s$	Laplace operator
$t$	time
$T$	transformation matrix
$T_d$	disturbance torque
$T_s$	sample/processing time
$T_{em}$	electromagnetic torque
$\theta_c$	instantaneous phase of carrier signal response
$\theta_{cmax\_A}, \theta_{cmax\_B}$	phases of carrier signal response waveform maximums
$\theta_r$	rotor position in electric [deg.]
$\theta_{r,meas}$	measured rotor position in electric [deg.]
$\theta_{rm}$	rotor position in mechanical [deg.]
$\theta_{error}$	rotor position error in electric [deg.]
$\Delta\hat{\theta}$	angular offset
$\vartheta$	phase shift due to cross-saturation in electric [deg.]
$\mathbf{u}$	scalar manipulated input vector
$\underline{u}_{\alpha\beta\_c}$	complex HFI rotary voltage vector
$\mathbf{u}_{\alpha\beta\_c}$	scalar HFI rotary voltage vector in stationary ( $\alpha\beta$ ) reference frame
$\mathbf{u}_{dq\_c}$	scalar HFI rotary voltage vector in rotary ( $dq$ ) reference frame
$U_c$	HFI voltage magnitude
$\underline{u}_{dq,AC} = u_{d,AC} + ju_{q,AC}$	alternating test signal voltage vector in rotary ( $dq$ ) reference frame
$\underline{u}_{dq,DC} = u_{d,DC} + ju_{q,DC}$	static operating point voltage vector in rotary ( $dq$ ) reference frame
$\underline{u}_{dq,M} = u_{d,M} + ju_{q,M}$	current vector in rotary ( $dq$ ) reference frame for motoring operation
$\underline{u}_{dq,G} = u_{d,G} + ju_{q,G}$	voltage vector in rotary ( $dq$ ) reference frame for generating/breaking operation
$\underline{V}_{\alpha\beta}$	generic vector in stationary ( $\alpha\beta$ ) reference frame
$v_i$	generic injection voltage
$\omega_r$	angular rotor velocity in electric [rad/s]
$\bar{\omega}_r$	average angular rotor velocity in electric [rad/s]
$\omega_{rm}$	angular rotor velocity in mechanical [rad/s]

---

$\omega_{rmL}$	filtered angular rotor velocity in mechanical [rad/s]
$\omega_{rmR}$	regular angular rotor velocity in mechanical [rad/s]
$\omega_c$	carrier frequency in electric [rad/s]
$\omega_n$	negative sequence angular frequency in electric [rad/s]
$\omega_p$	positive sequence angular frequency in electric [rad/s]
$\omega^*$	desired bandwidth in [rad/s]
$\omega_{BW}$	bandwidth in [rad/s]
$\omega_H$	high pass filter bandwidth in [rad/s]
$\omega_L$	low pass filter bandwidth in [rad/s]
$x_0$	initial condition state vector
$\xi$	anisotropy ratio
$y$	output vector
$\chi$	generic saliency ratio