

Haoyue Zerbe

**Modeling of Laser Welding  
with the Smoothed Particle  
Hydrodynamics Method**



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# **Modeling of Laser Welding with the Smoothed Particle Hydrodynamics Method**

Von der Fakultät Konstruktions-, Produktions- und Fahrzeugtechnik  
der Universität Stuttgart  
zur Erlangung der Würde einer Doktor-Ingenieurin (Dr.-Ing.)  
genehmigte Abhandlung

vorgelegt von  
**Haoyue Zerbe (geb. Hu)**  
aus Jiangsu

Hauptberichter: Prof. Dr.-Ing. Prof. E.h. Peter Eberhard  
Mitberichter: Prof. Dr. phil. nat. Thomas Graf

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Internet: [www.shaker.de](http://www.shaker.de) • e-mail: [info@shaker.de](mailto:info@shaker.de)

## Preface

This thesis is the result of my research at the Institute of Engineering and Computational Mechanics (ITM) at the University of Stuttgart. A major part of the research was performed in cooperation with the Institut für Strahlwerkzeuge (IFSW) in a joint German Research Foundation (DFG) project on “Modelling of the capillary in laser beam penetration welding with the Smoothed Particle Hydrodynamics Method”.

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Böblingen, February 2020

Haoyue Zerbe



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