

**Christian Posthoff, Bernd Steinbach**

**Trigonometry**

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Christian Posthoff  
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Berichte aus der Mathematik

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Shaker Verlag  
Düren 2020

**Bibliographic information published by the Deutsche Nationalbibliothek**

The Deutsche Nationalbibliothek lists this publication in the Deutsche Nationalbibliografie; detailed bibliographic data are available in the Internet at <http://dnb.d-nb.de>.

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Printed in Germany.

ISBN 978-3-8440-7447-5

ISSN 0945-0882

Shaker Verlag GmbH • Am Langen Graben 15a • 52353 Düren

Phone: 0049/2421/99011-0 • Telefax: 0049/2421/99011-9

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# Inhaltsverzeichnis

<b>1</b>	<b>Introduction</b>	<b>5</b>
1.1	The Definition of an Angle . . . . .	5
<b>2</b>	<b>The Angle Functions</b>	<b>7</b>
2.1	The Behavior of the Functions in the Four Quadrants . . . . .	13
2.2	The inverse functions . . . . .	16
2.3	Sum Formulas . . . . .	17
<b>3</b>	<b>Goniometric Equations</b>	<b>21</b>
<b>4</b>	<b>The Sine and Cosine Theorem</b>	<b>23</b>
4.1	Examples for the Calculation of Oblique Triangles . . . . .	23
4.2	Calculations on the Parallelogram and on the Trapezium	27
4.3	The Calculation of Important Parameters of the Triangle	28
4.3.1	The Heights in a Triangle . . . . .	28
4.3.2	The Bisectors of a Triangle . . . . .	29
4.3.3	The Medians in the Triangle . . . . .	29
4.3.4	The Diameter of the Circumcircle . . . . .	30
4.3.5	The Radius of the Inscribed Circle . . . . .	30
4.3.6	The Radius of the Outer Circles . . . . .	31
4.3.7	The Area of the Triangle . . . . .	31
4.3.8	The Tangential Theorem . . . . .	31
4.3.9	Mollweid's Formula . . . . .	32
4.4	Logarithmic Calculations of the Triangle . . . . .	32
<b>5</b>	<b>Complex Numbers - Operations with them</b>	<b>37</b>
5.1	Gauß' Number Plane . . . . .	37
5.2	Quadratic Equations . . . . .	39
<b>6</b>	<b>Hyperbolic Functions und their Inverses</b>	<b>41</b>
6.1	Hyperbolic Functions . . . . .	41

<b>7 Practical Tasks</b>	<b>45</b>
7.1 Roof Constructions and Moments of Inertia . . . . .	45
7.2 Curves in Polar Coordinates . . . . .	46
7.2.1 The Cardioid (Heart Curve) . . . . .	47
7.2.2 The Four Leaves . . . . .	48
7.2.3 The Lemniscate . . . . .	48
7.2.4 Pascal's Spiral . . . . .	49
7.2.5 The Strophoid . . . . .	49
7.2.6 The Cissoid . . . . .	50
7.2.7 Descartes' Leave . . . . .	51
7.3 The Calculation of Angles between Planes . . . . .	51